

Multi-knowledge Extraction from Violent Crime Datasets Using Swarm Rough Algorithm

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Abstract—This paper presents a swarm rough approach to analyze the combination factors of violent crime. The approach discovers the feature combinations in an efficient way to observe the change of rough set positive region as the fuzzy swarm proceed throughout the search space. We evaluated the performance of our approach using the violent factor datasets and the corresponding computational experiments are discussed. Empirical results indicate that our approach is ideal for all the considered problems and the fuzzy swarm optimization technique outperforms dynamic reducts (DR) approaches by obtaining multiple reductions for the combination factor datasets.

Keywords-Rough sets; Swarm intelligence, Fuzzy swarm optimization; Multi-knowledge extraction; Violent behavior analysis

I. INTRODUCTION

Violent crimes take violence behaviors of infringing upon other people to obtain some interest or satisfy a certain desire, including eight categories of violence cases: murder, explosion, poisoning, arson, hijacking, kidnapping, rape and intentional injury [1]. It not only causes severely victims' bodily injury and psychological trauma, but also seriously harms victims' families and public stability. The incidence rate of violent crimes is small, however, its social harmfulness is much severer than other crimes, so to prevent violent crimes are the focus of police work. Therefore, to explore the reasons of violent crime and the search for effective management and educational measures have been the key areas of sociology and criminology research. Currently, in the field of bioinformatics, a large number of genes about criminal factors have been excavated, which have the meaning of the milestone for the key of the detecting crime [2], [3], [4], [5]. At the same time, psychology has also been widely applied to the correlation analysis of crime factors, and it reveals the implicit relation between psychological motives. For example, the personality can be analyzed by the Eysenck Personality Questionnaire (EPQ) [6], [7]. In addition, some new information is obtained, such as the offender's personal information, crime, health and family background. These associated datasets imply some valuable

information. But they are acquired from measurements or from human experts, with uncertain and noisy information. So it is still an important challenge to analyze these datasets from practical and theoretical perspectives [8], [9], [10]. In this paper, we present an analytical framework analyze combination factors for violent crime and introduce a fuzzy swarm rough set approach to extract the rules from the multi-dimension factor datasets.

II. ANALYTICAL FRAMEWORK

In our violent behavior analysis, there are seven main steps: data acquisition, original datasets, data preprocessing, result analysis, normalizing datasets, data analysis, rules and conclusions. In the data acquisition step, we obtain three kinds of data attributes including the environment data, psychology data and genotype data. All the data are collected into the original datasets. The detailed attributes will be presented in Section V. There are some duplicates, deletion, dispersion and manifest fault, etc in the original data. We have to preprocess these data by cleaning, transforming, integration and filtering and then all the "clean" and "integrated" data are stored as normalized datasets. We statistically analyze the dataset. Their information entropy is measured. Then the proposed fuzzy rough set reduction is introduced to reduce the dataset. The reduction results are analyzed locally (single attribute or combination of several attributes) and globally (all attributes in one record or all records). The last step produces the output of some rules and conclusions. In summary, the complete system architecture is illustrated in Figure 1.

III. ROUGH SET REDUCTION

The basic concepts of rough set theory and its philosophy are presented and illustrated with examples in [11], [12], [13], [14], [15], [16]. Here, we illustrate only the relevant basic ideas of rough sets that are relevant to the present work.

In rough set theory, an information system is denoted in 4-tuple by $S = (U, A, V, f)$, where U is the uni-

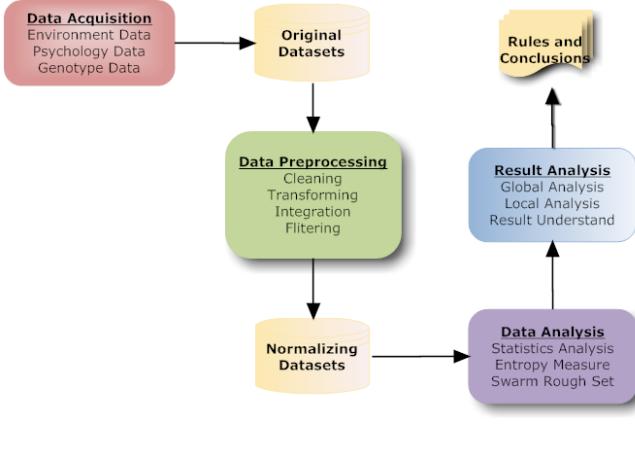


Figure 1. Overview of our architecture.

verse of discourse, a non-empty finite set of N objects $\{x_1, x_2, \dots, x_N\}$. A is a non-empty finite set of attributes such that $a : U \rightarrow V_a$ for every $a \in A$ (V_a is the value set of the attribute a).

$$V = \bigcup_{a \in A} V_a$$

$f : U \times A \rightarrow V$ is the total decision function (also called the information function) such that $f(x, a) \in V_a$ for every $a \in A, x \in U$. The information system can also be defined as a decision table by $T = (U, C, D, V, f)$. For the decision table, C and D are two subsets of attributes. $A = \{C \cup D\}$, $C \cap D = \emptyset$, where C is the set of input features and D is the set of class indices. They are also called condition and decision attributes, respectively.

Definition 1: [Reduct] Given a decision table $T = (U, C, D, V, f)$. The attribute $a \in B \subseteq C$ is $D - dispensable$ in B , if $POS_B(D) = POS_{(B-\{a\})}(D)$; otherwise the attribute a is $D - indispensable$ in B . If all attributes $a \in B$ are $D - indispensable$ in B , then B will be called $D - independent$. A subset of attributes $B \subseteq C$ is a $D - reduct$ of C , iff $POS_B(D) = POS_C(D)$ and B is $D - independent$.

Definition 2: [Multi-reduct] Let $2^{|A|}$ represent all possible attribute subsets $\{\{a_1\}, \dots, \{a_{|A|}\}, \{a_1, a_2\}, \dots, \{a_1, \dots, a_{|A|}\}\}$. Let RED represent the set of reducts, i.e.,

$$RED = \{B | POS_B(D) = POS_C(D), \\ POS_{(B-\{a\})}(D) < POS_B(D)\} \quad (1)$$

Definition 3: [Multi-knowledge] Let RED represent the set of reducts, and φ is a mapping from the condition space to the decision space. Then multi-knowledge can be defined as follows:

$$\Psi = \{\varphi_B | B \in RED\} \quad (2)$$

Definition 4: [Reduced positive universe] Given a decision table $T = (U, C, D, V, f)$. Let $U/C = \{[u'_1]_C, [u'_2]_C, \dots, [u'_m]_C\}$, reduced universe U' can be written as:

$$U' = \{u'_1, u'_2, \dots, u'_m\}. \quad (3)$$

And reduced positive universe U'_{pos} can be determined:

$$U'_{pos} = \{u'_{i_1}, u'_{i_2}, \dots, u'_{i_t}\}. \quad (4)$$

Definition 5: [Reduced positive region] Given a decision table $T = (U, C, D, V, f)$. Let $POS_C(D) = [u'_{i_1}]_C \cup [u'_{i_2}]_C \cup \dots \cup [u'_{i_t}]_C$, where $\forall u'_{i_s} \in U'$ and $|[u'_{i_s}]_C/D| = 1 (s = 1, 2, \dots, t)$. $\forall B \subseteq C$, reduced positive region

$$POS'_B(D) = \bigcup_{X \in U'/B \wedge X \subseteq U'_{pos} \wedge |X/D|=1} X \quad (5)$$

where $|X/D|$ represents the cardinality of the set X/D .

Consider Definitions 4 and 5, $\forall B \subseteq C$, $POS_B(D) = POS_C(D)$ if $POS'_B = U'_{pos}$ [16]. It is to be noted that U' is the reduced universe, which usually would reduce the scale of datasets significantly. It provides a more efficient strategy to observe the change of positive region when we search the reducts. We do not have to calculate $U/C, U/D, U/B, POS_C(D), POS_B(D)$ to compare $POS_B(D)$ with $POS_C(D)$ to determine whether they are equal to each other or not. We only calculate $U/C, U', U'_{pos}, POS'_B$ and then compare POS'_B with U'_{pos} .

IV. FUZZY SWARM ROUGH SET REDUCTION

As mentioned above, finding all the reducts of information systems or decision tables is NP-complete problem [17], [18]. In this section, we present a fuzzy swarm algorithm for rough set reduction.

A. Canonical swarm optimization

The canonical swarm model consists of a swarm of individuals, which are initialized with a population of random candidate solutions. They move iteratively through the d -dimension problem space to search the new solutions, where the fitness, f , can be calculated as the certain qualities measure.

Each individual has a position represented by a position-vector \vec{p}_i (i is the index of the individual), and a velocity represented by a velocity-vector \vec{v}_i . Each individual remembers its own best position so far in a vector $\vec{p}_i^\#$, and its j -th dimensional value is $p_{ij}^\#$. The best position-vector among the swarm so far is then stored in a vector \vec{p}^* , and its j -th dimensional value is p_j^* . During the iteration time t , the update of the velocity from the previous velocity to the new velocity is determined by Equ. (6). The new position is then determined by the sum of the previous position and the new velocity by Equ. (7).

$$v_{ij}(t) = wv_{ij}(t-1) + c_1 r_1(p_{ij}^\#(t-1) - p_{ij}(t-1)) \\ + c_2 r_2(p_j^*(t-1) - p_{ij}(t-1)) \quad (6)$$

$$p_{ij}(t) = p_{ij}(t-1) + v_{ij}(t) \quad (7)$$

where w is called as the inertia factor, r_1 and r_2 are the random numbers, which are used to maintain the diversity of the population, and are uniformly distributed in the interval $[0,1]$ for the j -th dimension of the i -th individual. c_1 is a positive constant, called as coefficient of the self-recognition component, c_2 is a positive constant, called as coefficient of the social component.

B. Fuzzy swarm for rough set reduction

Given a decision table $T = (U, C, D, V, f)$, the set of condition attributes, C , consist of m attributes. We set up a search space of m dimension for the rough set reduction.

Accordingly, each individual's position is represented as a vector with m dimension. Each dimension of the individual's position maps one condition attribute. The individual's position is a series of priority levels of the attributes. The sequence of the attribute will not be changed during the iteration. The domain for each dimension is limited from 0 to 1. The value '1' means the corresponding attribute is selected definitely while '0' not selected definitely. Otherwise the attribute would be selected with the probability according to the value of the individual's position. So each position can be "decoded" to a potential reduction solution, an subset of C . In other words, we can map C into a fuzzy set R using a fuzzy reduct relation through the individual's fuzzy position-vector. The fuzzy reduct relation \vec{p}_i between C and R has the following meaning: for each element in the position-vector \vec{p}_i (i is the index of the individual), the element

$$p_{ij} = \mu_F(C_j, R_j) \quad (8)$$

where μ_F is the membership function, $i \in \{1, 2, \dots, n\}$, $j \in \{1, 2, \dots, m\}$. In the attribute reduction problem, the elements of the solution must satisfy the following conditions:

$$p_{ij} \in [0, 1], i \in \{1, 2, \dots, n\}, j \in \{1, 2, \dots, m\} \quad (9)$$

Here p_{ij} represents the degree of membership of the i -th element c_i in domain C and the j -th element r_j in domain R to relation \vec{p}_i .

In the crisp mode, the individual's position in the considered dimension is positive, the corresponding attribute is selected definitely. And the negative direction implies that it is not selected definitely. In the fuzzy mode, the individual's position is fuzzified, which is propagated from its velocity. At each time iterating step, each individual updates its velocity according to Equ. (6). And the position is updated according to Equ. (7). In our fuzzy swarm model, the position is fuzzified by the sigmoid function:

$$\Gamma(p_{ij}(t)) = \frac{1}{1 + e^{-p_{ij}(t)}} \quad (10)$$

Figure 2 illustrates how the position is reacted on by its velocity when the individuals' maximum positions output

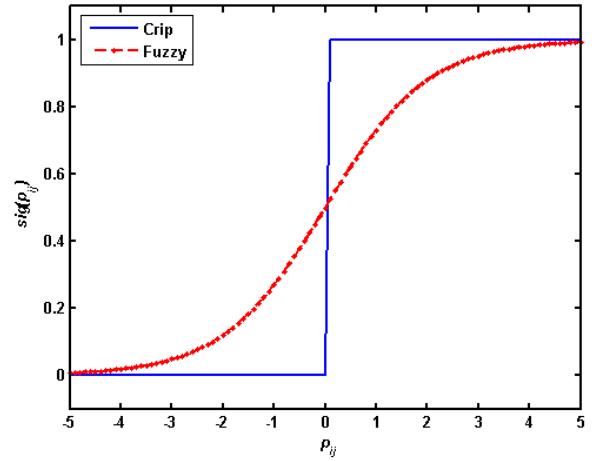


Figure 2. Curve of membership functions.

from Equ. (7) are clamped in between $[-5, 5]$. The membership functions are similar with the ones in [19].

Since the position indicates the potential reduction solution, we should "decode" the fuzzy vectors and get the feasible solutions. The position values are compared with a random number ρ in the interval $[0,1]$. If the position value is larger than ρ , the position would be defuzzied as '1', i.e. the corresponding selection flag $s_{ij}(t)$ is set to '1'. And the corresponding attribute with the position is selected. Otherwise the attribute would be not selected as Equ. (11). After all the elements of the position vector have been processed, we get the reduction solution from the fuzzy swarm model.

$$s_{ij}(t) = \begin{cases} 1 & \text{if } \Gamma(p_{ij}(t)) > \rho; \\ 0 & \text{otherwise.} \end{cases} \quad (11)$$

If it is a feasible solution, we calculate the attribute number in the subset of attributes. The solution with the lowest number would be selected. For the swarm, the lower number of attributes in the feasible solution, the better the fitness of the corresponding individual is. So the individual's fitness is determined by Equ. (12). If the reduced universe of discourse is non-equal to the reduced positive region, i.e. $POS'_E \neq U'_{pos}$, the fitness is punished as the total number of the condition attributes, otherwise the fitness is the attribute number of the potential reduction solution represented by the individual's position.

$$f_D(E) = \begin{cases} |E| & \text{if } POS'_E(D) = U'_{pos} \\ |C| & \text{if } POS'_E(D) \neq U'_{pos} \end{cases} \quad (12)$$

Algorithm 1 Fuzzy swarm rough set reduct algorithm

Input:

Swarm size n , the maximum velocity of individual swarm v_{max} , the component coefficients c_1 and c_2 .

Output:

Reduction solutions indicated by the vectors of the best individuals \vec{p}^* .

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1: Calculate  $U'$ ,  $U'_{pos}$  using Equs. (3) and (4);
2: Initialize the positions and the velocities for all the
   individuals randomly;
3: while the end criterion is not met do
4:    $t \leftarrow t + 1$ ;
   { // Calculate the fitness value of each individual}
5:   for  $i = 1$  to  $n$  do
6:     if  $POS'_E \neq U'_{pos}$  then
7:       the fitness is punished as the total number of the
          condition attributes;
8:     else
9:       the fitness is the number of '1' in the correspond-
          ing selection flag string  $\vec{s}_i(t)$ .
10:    end if
11:   end for
12:    $\vec{p}^* = argmin_{i=1}^n (f(\vec{p}^*(t - 1)), f(\vec{p}_1(t)), f(\vec{p}_2(t)), \dots, f(\vec{p}_i(t)), \dots, f(\vec{p}_n(t)))$ ;
13:   for  $i = 1$  to  $n$  do
14:      $\vec{p}_i^\#(t) = argmin_{i=1}^n (f(\vec{p}_i^\#(t - 1)), f(\vec{p}_i(t))$ ;
15:     for  $j = 1$  to  $d$  do
16:       Update the  $j$ -th dimension value of  $\vec{v}_i$  and  $\vec{p}_i$ 
          according to Equs. (6) and (7).
17:       Fuzzify the  $j$ -th dimension value of  $\vec{p}_i(t)$  by Equ.
          (10).
18:       Obtain the corresponding selection flag  $s_{ij}(t)$  by
          Equ. (12).
19:     end for
20:   end for
21: end while
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V. EXPERIMENTS AND RESULTS

A. Dataset acquiring

The dataset is acquired by the Chongqing Municipal Public Security Bureau, Institute of Environmental Systems Biology and School of Information Science and Technology of Dalian Maritime University. All informed consents were obtained before participation. During the acquiring process of dataset, the considered factors include the family environment (degree of education, occupation, and family economic status), P and N psychological factor, MAOA and DRD4 genotypes, up to 64 factors. The family environment information is acquired by participant's information questionnaire. The psychological information is obtained by Eysenck personality questionnaire. Genetic information is obtained by polymerase chain reaction (PCR).

Table II
PARAMETER SETTINGS FOR THE ALGORITHMS.

Algorithm	Parameter name	Value
DR	Number of sampling levels	5
	Number of subtables to sample per level	10
	Smallest subtable size (lowest level)	50%
	Largest substable size (highest level)	90%
Swarm	Swarm size	(even)(int)(10 + 2 * sqrt(L))
	Self coefficient c_1	$0.5 + log(2)$
	Social coefficient c_2	$0.5 + log(2)$
	Inertia weight w	0.91
	Clamping Coefficient ϕ	0.5

In the process of data acquisition, there are some missing, redundant and even data with some tolerances. There are three processing methods for handling these type of data records: no processing, filling or deleting. After cleaning, transforming, integration and filtering, the datasets are original 67 attributes (columns) and 2486 records (rows) to normalized 20 attributes (columns) and 578 records (rows) as illustrated in Table I.

B. Rough set extraction

After the normalized datasets are discretized, we make an attempt to reduce the datasets of combination factors using the proposed fuzzy swarm rough set algorithm. In our experiments, the algorithm used for comparison was dynamic reducts (DR) [20], [21]. Dynamic reducts (DR) is first defined by Bazan et al. [20], [21]. A number of subtables are randomly sampled from the input table, and proper reducts are computed from each of these using some algorithms. The reducts that occur the most across subtables are in some sense the "most stable" [22]. Both methods are valid and efficient in rough set reduction field due to their strong convergence properties. Our algorithms were implemented in the C++ language and their parameters settings are chosen in accordance with the recommendations of Clerc [23] and Liu [24]. The computation environment was an Intel® Core™ Duo CPU T2250 @1.73 GHz processor with 1G memory. Specific parameter settings for the algorithms are described in Table II, where L is the length of condition attributes. Each experiment (for each algorithm) was repeated 10 times with different random seeds. The average fitness values of the best solutions throughout the optimization run were recorded. The average number of surplus property and the number of optimal solutions in 10 trials are shown in Figure 3. The fuzzy swarm algorithm usually achieves better results than DR method. In addition, multiple fuzzy swarm usually produces multiple candidate reducts, allowing for the possibility of multi-knowledge extraction.

Table I
DATASET CLEANING.

Item	Before Preprocessing				After Preprocessing			
	Environment	Psychology	Genotype	Total	Family	Psychology	Genotype	Total
Column Record	63 1233	2 1233	2 2486	67 2486	16 578	2 578	2 578	20 578

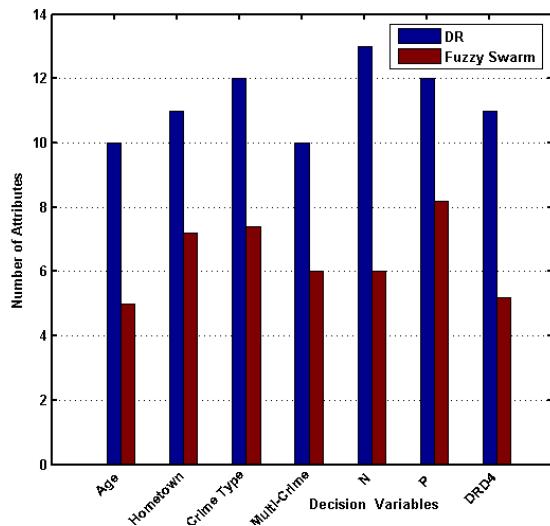


Figure 3. Number of attributes depending on decision variables.

According to the experimental data and results, the following rules are extracted:

- 1) The characteristics of the young-offenders are as follows, especially these from the single-parent family: economic condition is in the low middle level; EPQ-P score is high; junior high school educational level; DRD4 is middle-sized and MAOA is the third type or the fourth. The confidence is 79%.
- 2) The characteristics of the minority nationality are as follows: education level is low; unemployed; economic condition is poor and EPQ-P is the middle score or the high. The confidence is 72%.
- 3) The characteristics of the adult-offenders from east of Chongqing are as follows: EPQ-N score is middle or high and most of their educational level is highly-educated. The confidence is 68%.
- 4) The characteristics of the prisoners are as follows: DRD4 is abnormal; EPQ-P and EPQ-N scores are middle or high; MAOA is the fifth type and economic condition is the lower middle level and some are unemployed. The confidence is 65%.
- 5) The characteristics of the prisoners are as follows: they are bibulous; EPQ-P score is middle or high; economic

condition is in the lower middle level; term of penalty is longer and DRD4 is abnormal, most of them are from east of Chongqing. The confidence is 70%.

- 6) The characteristics of the adult-offenders are as follows: their childhood is abused; EPQ-P and EPQ-N scores are middle or high; economic condition is in the lower middle level and some are unemployed; term of penalty is longer and educational level is junior high school. The confidence is 71%.

These results are helpful to further understand the factors of violent crime.

VI. CONCLUSIONS AND FURTHER WORKS

This paper presented a novel fuzzy swarm rough set to analyze three kinds of combination factors, i.e. psychological, environmental and genetic factors. We evaluated the performance of our approach using the violent factor datasets and the corresponding computational experiments. Empirical results indicate that our approach is ideal for all the considered problems and the fuzzy swarm optimization technique outperformed the dynamic reducts (DR) approach by obtaining multiple reductions for the combination factor datasets. Although some knowledges should be analyzed and verified the correctness by neuroscientists further, the approach is helpful for violent behavior analysis. More methods [25-27] and some detailed underlying mechanism should be investigated further.

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